

Projectile Motion

Horizontally - velocity is constant

horizontal $\rightarrow V = \frac{\Delta d}{\Delta t}$ \leftarrow horizontal

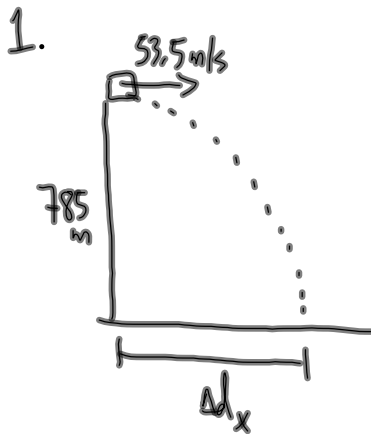
Vertically - constant acceleration ($a = -9.81 \text{ m/s}^2$)

$a = \frac{\Delta V}{\Delta t}$ and $V_{ave} = \frac{\Delta d}{\Delta t}$ \leftarrow vertical

Maybe Useful:

$$\left. \begin{aligned} \Delta d &= v_1 \Delta t + \frac{1}{2} a (\Delta t)^2 \\ \Delta d &= v_2 \Delta t - \frac{1}{2} a (\Delta t)^2 \\ v_2^2 &= v_1^2 + 2a \Delta d \end{aligned} \right\} \text{all vertical!}$$

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Vertically (constant acceleration)

$$\begin{aligned} \Delta d &= -785 \text{ m} \\ v_1 &= 0 \\ a &= -9.81 \text{ m/s}^2 \\ \Delta t &= ? \end{aligned}$$

$$\Delta d = v_1 \Delta t + \frac{1}{2} a (\Delta t)^2$$

$$\Delta d = \frac{1}{2} a (\Delta t)^2$$

$$\Delta t = \sqrt{\frac{2 \Delta d}{a}}$$

$$\Delta t = \sqrt{\frac{2(-785 \text{ m})}{-9.81 \text{ m/s}^2}}$$

$$\Delta t = 12.7 \text{ s}$$

Horizontally (constant v)

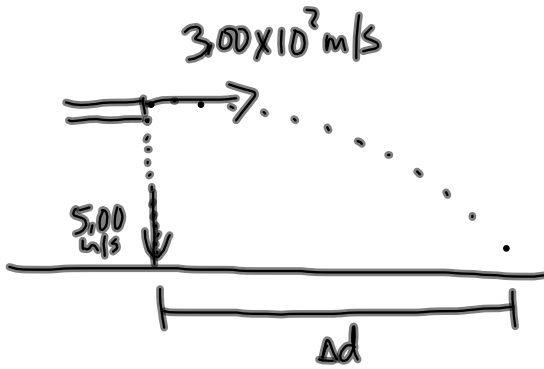
$$v = \frac{\Delta d}{\Delta t}$$

$$\Delta d = v \Delta t$$

$$\Delta d = (53.5 \text{ m/s})(12.7 \text{ s})$$

$$\Delta d = 677 \text{ m}$$

8.



Shell casing (vertically)

$$v_1 = 0$$

$$v_2 = -5.00 \text{ m/s}$$

$$a = -9.81 \text{ m/s}^2$$

$$\Delta t = ?$$

$$a = \frac{\Delta v}{\Delta t}$$

$$\Delta t = \frac{\Delta v}{a}$$

$$\Delta t = \frac{-5.00 \text{ m/s} - 0}{-9.81 \text{ m/s}^2}$$

$$\boxed{\Delta t = 0.510 \text{ s}}$$

a) Δd (horizontally) = ?

b) v_2 (vertically) = ?

The bullet is in the air for the same time as the casing, so:

horizontally (v is constant)

$$v = \frac{\Delta d}{\Delta t}$$

$$\Delta d = v \Delta t$$

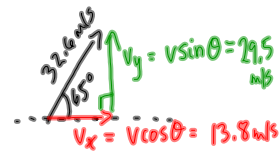
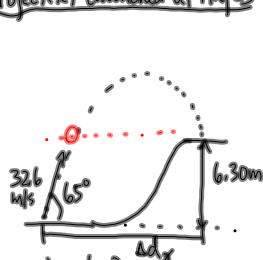
$$\Delta d = (3.00 \times 10^2 \text{ m/s})(0.510 \text{ s})$$

$$\boxed{\Delta d = 153 \text{ m}}$$



b) The vertical velocity of the bullet at impact is 5.00 m/s [down]

Projectiles launched at Angles



- a) $\Delta t = ?$
- b) Δd (horiz)
- c) V (at impact)

- a) vertically (constant acc)
 - $v_i = 29.5 \text{ m/s}$
 - $\Delta d = +6.30 \text{ m}$
 - $a = -9.81 \text{ m/s}^2$
 - $\Delta t = ?$

$$\Delta d = v_i(\Delta t) + \frac{1}{2}a(\Delta t)^2$$

$$+6.30 \text{ m} = (29.5 \text{ m/s})\Delta t - \frac{9.81 \text{ m/s}^2}{2}(\Delta t)^2$$

$$+ \frac{9.81 \text{ m/s}^2}{2}(\Delta t)^2 - (29.5 \text{ m/s})\Delta t + 6.30 \text{ m} = 0$$

- ① find roots by graphing $y = ax^2 + bx + c$
- ② use quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{29.5 \pm \sqrt{(29.5)^2 - 4\left(\frac{9.81}{2}\right)(+6.30)}}{2\left(\frac{9.81}{2}\right)}$$

$$x = \frac{29.5 \pm 27.4}{9.81}$$

on the way up \rightarrow

$$x = \frac{29.5 - 27.4}{9.81} \quad x = \frac{29.5 + 27.4}{9.81}$$

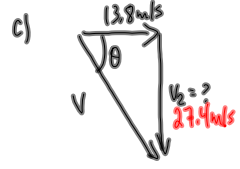
$$\boxed{x = 0.216 \text{ s}} \quad \boxed{x = 5.80 \text{ s}}$$

- b) horizontally (velocity is constant)

- $v = 13.8 \text{ m/s}$
- $\Delta t = 5.80 \text{ s}$
- $\Delta d = ?$

$$\Delta d = (13.8 \text{ m/s})(5.80 \text{ s})$$

$$\boxed{\Delta d = 80.0 \text{ m}}$$



$$v^2 = 27.4^2 + 13.8^2$$

$$\boxed{v = 30.7 \text{ m/s}}$$

$$\tan \theta = \frac{27.4 \text{ m/s}}{13.8 \text{ m/s}}$$

$$\boxed{\theta = 63.3^\circ}$$

vertically (constant acc)

- $v_i = 29.5 \text{ m/s}$
- $v_f = ?$
- $a = -9.81 \text{ m/s}^2$
- $\Delta t = 5.80 \text{ s}$

$$a = \frac{v_2 - v_1}{\Delta t}$$

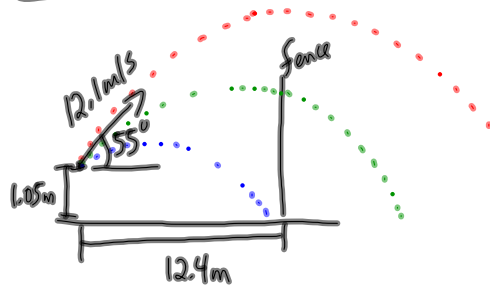
$$v_2 = v_1 + a\Delta t$$

$$v_2 = 29.5 \text{ m/s} - 9.81 \text{ m/s}^2(5.80 \text{ s})$$

$$\boxed{v_2 = -27.4 \text{ m/s}}$$

The velocity when the ball hits the ground is 30.7 m/s [63.3° below the horizontal]

MP/542



You need to find the height of the ball when it has travelled 12.4m horiz.

$$V_x = (12.1 \text{ m/s}) \cos 55^\circ = 6.94 \text{ m/s}$$

$$V_y = (12.1 \text{ m/s}) \sin 55^\circ = 9.91 \text{ m/s}$$

To find the time to travel 12.4m horizontally:

$$V_x = \frac{\Delta d_x}{\Delta t}$$

$$\Delta t = \frac{\Delta d_x}{V_x}$$

$$\Delta t = \frac{12.4 \text{ m}}{6.94 \text{ m/s}}$$

$$\Delta t = 1.79 \text{ s}$$

Find the height ($\Delta d_y + 1.05 \text{ m}$)

$$V_i = 9.91 \text{ m/s}$$

$$a = -9.81 \text{ m/s}^2$$

$$\Delta t = 1.79 \text{ s}$$

$$\Delta d = ?$$

$$\Delta d = V_i \Delta t + \frac{1}{2} a (\Delta t)^2$$

$$\Delta d = 9.91(1.79) - \frac{9.81}{2}(1.79)^2$$

$$\Delta d = 2.08 \text{ m}$$

$$h = 2.08 \text{ m} + 1.05 \text{ m} = 3.13 \text{ m}$$

Since $3.13 \text{ m} < 4.8 \text{ m}$, the ball hits the fence.

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